

$$66) \Delta P = -P \cdot \text{Mod } D \cdot \Delta i$$

$P = 1000$ since the bond is bought at par

$$\text{Mod } D = \text{Mac } D \cdot v = \frac{7.959}{1.072}$$

$$\Delta i = .08 - .072 = .008$$

$$\therefore \Delta P = -1000 \left(\frac{7.959}{1.072} \right) (.008) = -59.395 \dots$$

$$\therefore P^{\text{new}} = 1000 + \Delta P = 940.60$$

$$178) \quad \Delta P = P \left[\left(\frac{1.10}{1.1025} \right)^{11} - 1 \right]$$

$$\therefore \frac{\Delta P}{P} = \left(\frac{1.1}{1.1025} \right)^{11} - 1 = -0.02466 \dots$$

$$187) \quad \Delta P = -P \cdot M_{od} D \cdot \Delta i$$

$$M_{od} D = M_{ac} D \cdot v = \frac{11}{1.1} = 10$$

$$\therefore \frac{\Delta P}{P} = -10 \cdot (.0025) = -.025$$

$$188) \quad \Delta P = P \left[\left(\frac{1+i_{old}}{1+i_{new}} \right)^{MacD} - 1 \right]$$

$P = 1000$ since the bond is bought at par

$$\therefore \Delta P = 1000 \left(\left(\frac{1.072}{1.08} \right)^{7.959} - 1 \right) = -57.458 \dots$$

$$\therefore P^{new} = 1000 + \Delta P = 942.54$$

$$189) \text{ For } E_{MAC}, \Delta P = P \cdot \left(\left(\frac{1.064}{1.07} \right)^{MacD} - 1 \right)$$

$$MacD = 8(1.064) = 8.512$$

$$\therefore \Delta P = 112955 \left(\left(\frac{1.064}{1.07} \right)^{8.512} - 1 \right)$$

$$= -5279.255 \dots$$

$$\therefore E_{MAC} = 112955 + \Delta P = 107676$$

$$\text{For } E_{MOD}, \Delta P = -P \cdot ModD \cdot 4i = -112955(8)(.006)$$

$$= -5421.84$$

$$\therefore E_{MOD} = 112955 + \Delta P = 107533$$

$$\therefore E_{MAC} - E_{MOD} = 143$$

190) Using $i = .0432$, the portfolio has

$$P = 35000 + 65000 = 100000$$

$$MacD = 7.28 \left(\frac{35000}{100000} \right) + 12.74 \left(\frac{65000}{100000} \right) = 10.829$$

Using the new interest rate i , $\Delta P = 5000$

$$\therefore 5000 = 100000 \left(\left(\frac{1.0432}{1+i} \right)^{10.829} - 1 \right)$$

$$\Rightarrow i = .03851 \dots$$

$$191) \quad \Delta P = 121212 - 123000 = -1788$$

$$\therefore -1788 = 123000 \left(\left(\frac{1.05}{1.054} \right)^{\text{MacD}} - 1 \right)$$

$$\Rightarrow \text{MacD} = 3.85117 \dots$$

$$\therefore \text{Mod D} = \text{MacD} \cdot 2 = \frac{3.85117 \dots}{1.05} = 3.667 \dots$$